

1 **Deflection of O_2^+ ion flow by the Martian Magnetic Fields**

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14

15 **Abstract.**

16 The effect of the Martian crustal magnetic field on ion escape is the focus of considerable interest.
17 Directions of Martian magnetic field determined by the interaction between Mars' crustal and
18 interplanetary magnetic fields have been suggested to play a significant role on ion transport around
19 Mars. In this study we investigate the physical mechanism deflecting O_2^+ transport in two typical
20 magnetic field orientations at horizontal plane by performing three-dimensional multi-fluid Hall
21 magneto-hydrodynamic (MHD) simulations. Cross validation of the simulation results from G110
22 crustal field model and equivalent source dipole model reveals that due to the Hall electric force, O_2^+
23 ions flow tends to be accelerated eastwards in the region occupied by outward magnetic fields, and
24 westwards in the region with inward magnetic fields. These results are helpful for understanding how
25 the deflection of Martian atmospheric ions flow are influenced by the Martian magnetic field
26 environment and the impact of the crustal fields on the motion of atmospheric ions in the Martian
27 space environment.

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29

30 **Keywords**

31 Mars, Solar-planetary interactions, Magnetic anomalies, Magnetohydrodynamics

32

33 **1. Introduction**

34 The mechanisms that have caused the Martian atmosphere to evolve from Earth-like to the
35 present situation have been a topic of considerable debate since the first probes arrived at the planet.
36 Compared to the Earth, Mars is further away from the Sun and does not possess an intrinsic magnetic
37 field. Although the substantial intrinsic magnetic field on Earth can block high-energy particles in
38 solar wind and prevent planetary ions from escaping, the terrestrial magnetic field is not necessarily
39 needed to protect the planetary atmosphere from erosion by the solar wind (Ramstad et al., 2021).
40 Indeed, the presence of the intrinsic magnetic field appears to increase the ion escape rate for most
41 levels of magnetization and solar wind conditions (Gunell et al., 2018; Ramstad et al., 2021).
42 Furthermore, the relationship between the strength of the intrinsic magnetic field and the magnetic
43 standoff distance indicates that the relative position between the standoff distance and the induced
44 magnetosphere determines the enhancing/inhibiting effect of the intrinsic magnetic field on the ion
45 escape rate (Egan et al., 2019; Sakata et al., 2020).

46 Despite the fact that Mars lacks a global intrinsic magnetic field, it possesses local magnetic
47 fields on its surface, primarily distributed in the southern hemisphere with the strongest located at
48 east longitude around 180° (Acuña et al., 1999). The presence and asymmetric distribution of these
49 crustal fields introduce great complexity into the plasma dynamics of the Martian environment,
50 resulting in a disordered magnetic field topology (Xu et al., 2016; Weber et al., 2020). Observational
51 analysis reveals three magnetic field topologies in the Martian plasma environment, i.e., closed, open
52 and draped (Brain et al., 2007; Duru et al., 2011; Weber et al., 2020; Xu et al., 2017). Xu et al. (2019)
53 have suggested that below an altitude of 1200 km, the dominant magnetic topology over strong
54 crustal fields on the dayside is the so-called closed-to-day, with vertical magnetic field lines at two
55 ends embedded in the collisional atmosphere, between which horizontal magnetic field lines exist.
56 Previous studies have also shown that the direction of the magnetic field has a significant impact on
57 the ion transport. The diffusion of ionospheric plasma tends to be suppressed around the region
58 dominated with horizontal magnetic field lines, confirmed by 2D ionospheric simulations (Matta et
59 al., 2015). On the other hand, vertical magnetic field lines tend to promote plasma to high altitudes.

60 Based on observational analysis from the Mars Express (MEX) mission, hyperbola-shaped traces in
61 the echogram and dual traces in the ionogram have been repeatedly observed above regions with
62 vertical and strong crustal magnetic fields (e.g., Duru et al., 2006; Gurnett et al., 2005; Andrews et
63 al., 2014; Diéval et al., 2018), interpreted as indications of ionospheric upwelling. This has been
64 demonstrated to be a result of field-aligned plasma diffusion and characterized by an increase in
65 electron density (Matta et al., 2015). Meanwhile, by statistically analyzing data from Mars
66 Atmosphere and Volatile Evolution (MAVEN) mission, Wu et al (2019) have confirmed that vertical
67 magnetic field lines tend to cluster around strong magnetic anomalies on Mars and the ion
68 distributions for near-vertical field lines are more extended than those for near-horizontal field lines.
69 Moreover, the global-scale ion transport around Mars can also be affected by the crustal field in the
70 horizontal plane, causing deflection of the ion flows in the southern hemisphere (Fan et al., 2020).

71 While the previously reported results show that there exists a strong dependence between the
72 magnetic field direction and ion transport, the physical mechanism behind this phenomenon is not
73 fully understood, especially the deflection effect due to Martian crustal field in the horizontal plane.
74 While there have been many models in order to study the interaction between solar wind and Mars
75 (e.g., Ma et al., 2004; Najib et al., 2011; Dong et al., 2014; Li Y. et al., 2021) and the impact of crustal
76 magnetic fields on modifying global Martian ion escape rate (e.g., Fang et al., 2015, 2017), few self-
77 consistent global simulations of Mars-solar wind interaction devote to resolve the physical
78 mechanism of the impact of magnetic field orientations on the ion transport deflection. In this study,
79 by investigating the ion dynamics and electromagnetic forces in the regions occupied by the Martian
80 crustal magnetic field, we show how two typical orientations of the magnetic field affect plasma
81 transport around Mars. Our results contribute to the understanding of how the deflecting direction of
82 Martian atmospheric ions flow is influenced by the orientation of magnetic field.

83 **2. Model Description**

84 The 3-D multi-fluid MHD Model used in this study solves separate mass, momentum and energy
 85 equations for the four main ion species in the Martian ionosphere, i.e., H^+ , O_2^+ , O^+ , CO_2^+ . The
 86 governing equations for ion species s can be expressed as follows (Najib et al., 2011, Li et al., 2022):

$$87 \quad \frac{\partial \rho_s}{\partial t} + \nabla \cdot (\rho_s \mathbf{u}_s) = \frac{\delta \rho_s}{\delta t} \quad (1a)$$

$$88 \quad \frac{\partial (\rho_s \mathbf{u}_s)}{\partial t} + \nabla \cdot (\rho_s \mathbf{u}_s \mathbf{u}_s + \mathbf{I} p_s) = n_s q_s (\mathbf{u}_s - \mathbf{u}_+) \times \mathbf{B} + \frac{n_s q_s}{n_e e} (\mathbf{J} \times \mathbf{B} - \nabla p_e) + \frac{\delta M_s}{\delta t} \quad (1b)$$

$$89 \quad \frac{\partial e_s}{\partial t} + \nabla \cdot [(e_s + p_s) \mathbf{u}_s] = \mathbf{u}_s \cdot \left[n_s q_s (\mathbf{u}_s - \mathbf{u}_+) \times \mathbf{B} + \frac{n_s q_s}{n_e e} (\mathbf{J} \times \mathbf{B} - \nabla p_e) \right] + \frac{\delta E_s}{\delta t} \quad (1c)$$

90 where $e_s = \frac{1}{2} \rho_s \mathbf{u}_s^2 + \frac{p_s}{\gamma-1}$. Here ρ_s , \mathbf{u}_s , p_s , n_s and q_s are the individual mass density, velocity, pressure
 91 of the ions, number density and charge respectively. \mathbf{B} is the magnetic field, \mathbf{I} is the identity matrix,
 92 γ is the polytropic index chosen to be 5/3. $p_e = \sum_{i=ions} p_i$, $n_e = \sum_{i=ions} n_i$ are the pressure and
 93 number density of electrons. The electric current density can be obtained from $\mathbf{J} = \frac{1}{\mu_0} \nabla \times \mathbf{B}$.

94 The source terms $\frac{\delta \rho_s}{\delta t}$, $\frac{\delta M_s}{\delta t}$ and $\frac{\delta E_s}{\delta t}$ on the right side of Equation (1), respectively represent the
 95 variations of mass, momentum and energy due to the collisions and chemical reactions among all the
 96 species (Li et al., 2020), where the inelastic collisions include three chemical reactions of charge
 97 exchange, photoionization and recombination, with the corresponding reaction rates adopted from
 98 Ma et al., (2004) and Schunk and Nagy (2009). The photoionization effect was included by adopting
 99 the Chapman function method, which has been proved to significantly improve the agreement with
 100 the plasma density observations (Ma et al., 2015).

101 By introducing the charge-averaged ion velocity $\mathbf{u}_+ = \frac{1}{en_e} \sum_s n_s q_s \mathbf{u}_s$ and electron velocity $\mathbf{u}_e =$
 102 $\mathbf{u}_+ - \frac{\mathbf{J}}{en_e}$, the magnetic induction equation can be written as:

$$103 \quad \frac{\partial \mathbf{B}}{\partial t} - \nabla \times \left(\mathbf{u}_+ \times \mathbf{B} - \frac{\mathbf{J} \times \mathbf{B}}{en_e} + \frac{\nabla p_e}{en_e} \right) = 0 \quad (2)$$

104 It should be noted that the electromagnetic (EM) forces acting on the O_2^+ ion can be derived from
 105 the plasma momentum equations of Equation (1b), which has the form as follows:

$$106 \quad \mathbf{F}_{EMO_2^+} = n_s q_s (\mathbf{u}_s - \mathbf{u}_+) \times \mathbf{B} + \frac{n_s q_s}{n_e e} \mathbf{J} \times \mathbf{B} - \frac{n_s q_s}{n_e e} \nabla p_e \quad (3)$$

107 The three terms on the right side of Equation (3) respectively correspond to motional electric
 108 force, Hall electric force and ambipolar electric force. It is noteworthy that the magnetic field is
 109 moving with average ion velocity (\mathbf{u}_+), so the motional electric force on O_2^+ depends on its relative
 110 velocity to \mathbf{u}_+ (Ma et al., 2019).

111 The Mars-centered Solar Orbital (MSO) reference frame was adopted in our simulations, where
 112 the x axis points from Mars towards the Sun ($-24R_M \leq X_{MSO} \leq 8R_M$), the z axis is perpendicular to
 113 the x axis and positive toward the north celestial pole, the y axis completes the right-handed coordinate
 114 system ($-16R_M \leq Y_{MSO}, Z_{MSO} \leq 16R_M$). The total number of computational cells is 960,000 with
 115 the finest cell of 10 km at the lowest inner boundary. In case of analyzing the ion dynamics in the
 116 horizontal plane at a certain altitude, the spherical coordinates (r, θ, φ) transformed from the MSO
 117 was adopted where r points radially outward, θ points southward, and φ points eastward. According
 118 to the typical solar wind parameters in upstream of Mars (Dong et al., 2014; Liu et al., 2021), the
 119 solar wind density and velocity were chosen to be 4 cm^{-3} and 500 km/s, respectively. The IMF was
 120 assumed to be a Parker spiral orientation of 56° with magnitude of 3 nT in the x - y plane, i.e.,
 121 $(B_x, B_y, B_z) = (-1.6, 2.5, 0) \text{ nT}$ in the MSO coordinate system. We adopted the 110° harmonic
 122 expansion for the crustal magnetic field developed by Gao et al., (2021) to describe the observed
 123 fields at Mars (Acuña et al., 1999). The subsolar point is 180° longitude at the equator, corresponding
 124 to $(X_{MSO}, Y_{MSO}, Z_{MSO}) = (X, 0, 0)R_M$, where $1 \leq X \leq 8$.

125 Moreover, equivalent source dipole (ESD) is one of general methods for building the crustal
 126 magnetic field on Mars (Li X. Z. et al., 2020), and fits the observed magnetic field with an equivalent
 127 strength distribution of magnetic dipoles. The structure of the magnetic dipole is nearly the same as
 128 the closed-to-day topology that has two vertical-line regions at two ends embedded in Martian
 129 ionosphere, between which is the horizontal-line region in the center. Therefore, in order to verify the
 130 physical mechanism and impact of magnetic field orientations on O_2^+ deflecting direction, we placed
 131 an ESD below the surface of 180° longitude and -53° latitude with the equivalent strength of the real

132 strongest Martian anomaly to mimic closed-to-day magnetic field topology. Expressions of the
133 magnetic field for the ESD are as follows:

$$134 \quad B_x = 3(x - x_0)(y - y_0)M_y r^{-5}, \quad (4a)$$

$$135 \quad B_y = (3(y - y_0)^2 - r^2)M_y r^{-5}, \quad (4b)$$

$$136 \quad B_z = 3(z - z_0)(y - y_0)M_y r^{-5}, \quad (4c)$$

137 where M_y and r , respectively, denote the magnetic moment along the y axis and the altitude above
138 the Martian surface. The point (x_0, y_0, z_0) in the MSO coordinate represents the center of the dipole
139 field. The $M_y = 6 \times 10^{10} \text{ nT} \cdot \text{km}^3$ and $(x_0, y_0, z_0) = (1840 \text{ km}, 0, -2441 \text{ km})$ were chosen,
140 which means that the ESD is located at 53°S with roughly 180 nT magnitude at 350 km altitude,
141 which is approximately consistent with the observational value of the actual crustal magnetic field.
142 Figures in Appendix A provide the magnetic field topology of the ESD around Mars and the
143 distributions of the total magnetic field strength and inclination angle at 350 km, resulting from
144 observations and simulations with the crustal magnetic field representation of ESD and the Gao et al.
145 (2021) model, respectively.

146 **3. Simulation Results**

147 The O_2^+ ion is one of the dominant species in the Martian ionosphere (Withers et al., 2019; Inui
148 et al., 2019; Sakai et al., 2018) and ion transport is a critical factor in the ion escape mechanism at
149 Mars. On the one hand, at high altitude (above 200 km) ion transport dominates (Mendillo et al. 2011;
150 Chaufray et al. 2014) and the ion flow tends to be deflected by the crustal field in the horizontal plane
151 (Fan et al., 2020). On the other hand, the ion distribution can be affected by the diffusion process
152 associated with the orientation of magnetic field (Wu et al., 2019; Matta et al., 2015). In order to
153 demonstrate the deflection impact of Martian crustal magnetic field on the O_2^+ ion flow, we
154 transformed our numerical result from MSO coordinates into the spherical coordinates and extracted
155 dayside horizontal velocity vector (black) of O_2^+ ions mapped on the distribution of Martian crustal

156 field isomagnetic lines (grey) at 350 km, as shown in Figure 1, which was obtained from numerical
157 run with G110 model. It is obvious that the ion flow in the southern hemisphere is deflected to the
158 eastward/westward by the crustal magnetic fields and the magnitude is smaller than in the northern
159 hemisphere, which are consistent with previous observations (Fan et al., 2020). Since the distribution
160 of O_2^+ velocity in the northern and southern hemisphere are supposed to be equatorially symmetric in
161 absence of crustal field (shown in Appendix B), it is the Martian crustal fields that deflect the direction
162 of O_2^+ ions flow in the southern hemisphere. Moreover, the eastward and westward ions flows appear
163 alternately around the strongest crustal field region marked by a dashed orange rectangle. This feature
164 is similar to the orientation of Martian magnetic fields as shown in Appendix Figures A3(a) and A3(b),
165 both the observations and simulation confirm that the inward and outward magnetic fields are also
166 dominant alternatively in the same area. Therefore, it is reasonable to believe that there is a correlation
167 between the deflection direction of the O_2^+ ions flow and the orientation of the magnetic field.

168 The magnetic inclination angle, defined as the angle that the local total magnetic field vector
169 makes with the horizontal plane, was used to study the relevance of the deflection direction of ions
170 flow to their surrounding magnetic field environment. Large absolute value of magnetic inclination
171 angle presents vertical magnetic field whereas smaller one denotes near-horizontal field, additionally
172 positive value of magnetic inclination angle indicates outward magnetic field whereas negative values
173 means inward magnetic field. Figures 2a, 2b and 2c respectively show the variations of the eastward
174 O_2^+ velocity (U_ϕ), the magnetic inclination angle and eastward EM Forces (F_ϕ) exerted on O_2^+ ions at
175 350 km with latitude from -90° to 0° , extracted at longitude of 180° . The grey highlights in Figure
176 2 represents the strong crustal field region, corresponding to the center line of dashed orange rectangle
177 in Figure 1. From Figure 2(a) it can be seen that the U_ϕ changes from positive to negative, then to
178 positive with increasing latitude in the strong crustal field region, which shows a similar variation
179 tendency of magnetic field inclination angle as revealed by Figure 2(b). Additionally, in order to
180 analyze the EM forces acting on the ions in detail, the eastward components of the total forces
181 expressed as in Equation (3) were plotted in Figure 2c, which shows that the total F_ϕ is mainly
182 provided by the Hall electric force. Moreover, comparison between Figures 2(b) and 2(c) shows that

183 the magnetic inclination angle almost has the same sign as the total F_ϕ , especially in the strong crustal
184 field region. The similar variation tendency between U_ϕ , F_ϕ and magnetic inclination angle in the
185 strong crustal field region implies that the ion flow tends to be accelerated by the eastward EM forces
186 in the regions with outward magnetic field, while in the regions with inward magnetic field, ion flow
187 can be accelerated by the westward EM forces.

188 In order to figure out the correspondence between the orientation of magnetic field and the
189 direction of total EM F_ϕ exerted on O_2^+ ions. Here, we respectively defined regions with outward and
190 inward magnetic fields as with inclination angle higher than 10° and smaller than -10° . Figure 3
191 demonstrates the dayside southern hemisphere distribution of positive (Fig.3a) and negative (Fig. 3b)
192 total EM F_ϕ in latitude from 0° to -90° and longitude from 90° to 270° at altitude of 350 km,
193 superimposed by red and blue dashed contour lines with 10° and -10° magnetic inclination angle
194 respectively. Comparison of F_ϕ distribution for the two different types of magnetic field regions in
195 Figure 3 indicates that the positive F_ϕ dominates in the region with outward magnetic field, which
196 can speed up ions flow eastwards, while in the region with inward magnetic field, the negative F_ϕ is
197 dominant and can speed up ions flow westwards .

198 Due to the irregularity and narrow, strip-like distribution of the Martian crustal field, the regions
199 occupied by magnetic field with different orientations are difficult to distinguish (as shown in
200 Appendix Figures A3(a) and A3(b)), which motivated us to adopt a simplified dipole model to cross-
201 validate the roles and mechanisms of orientation of magnetic field in deflecting the ion transport.
202 Since the magnetic moment we adopted is along the y axis, there is an apparent outward (inward)
203 magnetic field region in the Martian western (eastern) hemisphere and these two regions have the
204 same magnetic field strength, which facilitates the clarification of the impact and mechanism of
205 orientations of magnetic field on the ion flow deflection.

206 Figure 4 shows the dayside O_2^+ velocity vector mapped on the distribution of magnetic
207 inclination angle in the horizontal plane at 350 km for the case with ESD model. It can be seen that
208 the pattern of O_2^+ ions flow in the northern hemisphere is similar to that in the case without crustal
209 field model (shown in Appendix B). The magnitude of O_2^+ velocity in the southern hemisphere is
210 smaller than the counterpart of the northern one, especially in the vicinity of the central position of
211 ESD. Meanwhile, O_2^+ flow deflects to eastward in the outward magnetic field region, marked with red
212 rectangle in Fig. 4, and westward in the inward magnetic field region with blue. Thus, the deflection
213 direction of O_2^+ ions flow in the horizontal plane depends on the orientation of magnetic fields.

214 Figure 5a demonstrates the distribution of magnetic inclination angle in latitude from -30° to
215 -60° and longitude from 160° to 200° at altitude of 350 km for the cases with ESD model. Figures
216 5b, 5c and 5d respectively show the variations of the magnetic inclination angle, the eastward O_2^+
217 velocity (U_φ) and eastward EM Forces (F_φ) exerted on O_2^+ ions with longitude, extracted at latitude
218 of -50° from Figure 5a (white line). We respectively defined outward and inward magnetic field
219 regions as with elevation angles higher and smaller than 0° , which are highlighted in Figures 5b to 5d
220 in orange and blue. U_φ and F_φ have opposite signs on either side, and are approximately zero in the
221 central position of ESD. In the outward field region with longitude of 160° to 180° , both U_φ and F_φ
222 are in the eastward direction, indicating that O_2^+ ions are being accelerated eastwards in this region.
223 In addition, both U_φ and F_φ are in the westward direction in the inward field region with longitude of
224 180° to 200° , indicating that O_2^+ ions are being accelerated westwards there. It can be seen from
225 Figure 5d that the dominant force in the φ direction is Hall electric force. Therefore, the simulation
226 results obtained by considering the ESD model reinforce the conclusions derived from the case with
227 G110 model.

228 **4. Discussion and Conclusion**

229 The well-developed MHD model employed in this study is able to self-consistently reproduce
230 the Martian ionosphere by including the production and loss processes of the main ionospheric ion

231 species through considering physical collisions and chemical reactions among these species. In order
232 to investigate the impact of orientations of magnetic field on O_2^+ ions flow deflection, Gao's crustal
233 field model (G110) and an equivalent source dipole (ESD) model with similar strength and position
234 of the strongest crustal field were adopted to cross-validate physical mechanisms behind the
235 phenomena with each other.

236 Results from numerical simulations indicate that there exists a strong correspondence between
237 the direction of O_2^+ ions transport and the orientation of magnetic field. Magnetic fields can deflect
238 the flow of O_2^+ ions, i.e., O_2^+ ions flow tends to be accelerated towards the east in the outward
239 magnetic field region and west in the inward one. The controlling force is mainly contributed by the
240 Hall electric force, which provides an explanation for the deflection effect of the Martian crustal fields
241 observed by MAVEN (Fan et al., 2020).

242 Although our simulation results revealed that the Hall electric field has a significant impact on
243 deflecting ions flow in the outward/inward magnetic field region, the distributions of O_2^+ velocity in
244 the northern and southern hemisphere at a certain altitude are equatorially symmetric in absence of
245 crustal field as shown in Appendix B, meaning that there is no deflection effect in the horizontal
246 magnetic field region formed by draping interplanetary magnetic field. In other words, only
247 outward/inward magnetic field formed by the interaction of interplanetary magnetic field and the
248 Martian crustal field deflects ions motion in the horizontal plane. Moreover, the orientation of the
249 interplanetary magnetic field and the rotation of the crustal field with Mars have a significant impact
250 on the Martian magnetic field environment, which in turn affects the ion motion and deserves further
251 investigation.

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260 **Figure captions**

261 Figure 1. Dayside O_2^+ ion velocity vector (black anchor) overlapped on isomagnetic lines (grey) of
262 the Martian crustal field in the horizontal plane at 350 km, resulting from simulation with Gao's
263 crustal field model.

264 Figure 2. Distributions of variables resulting from simulation with Gao's crustal field model at 350
265 km. The variation of (a) eastward velocity (U_ϕ), (b) magnetic field inclination angle, (c) eastward
266 total electro-magnetic forces (F_ϕ , red line) and Hall electric force (green line) along latitude at
267 longitude of 180° .

268 Figure 3. Dayside southern hemisphere distribution of positive (a) and negative (b) total EM F_ϕ in
269 latitude from 0° to -90° and longitude from 90° to 270° at altitude of 350 km accompanied by red
270 and blue dashed contour lines of 10° and -10° magnetic inclination angle separately, resulting from
271 simulation with Gao's crustal field model.

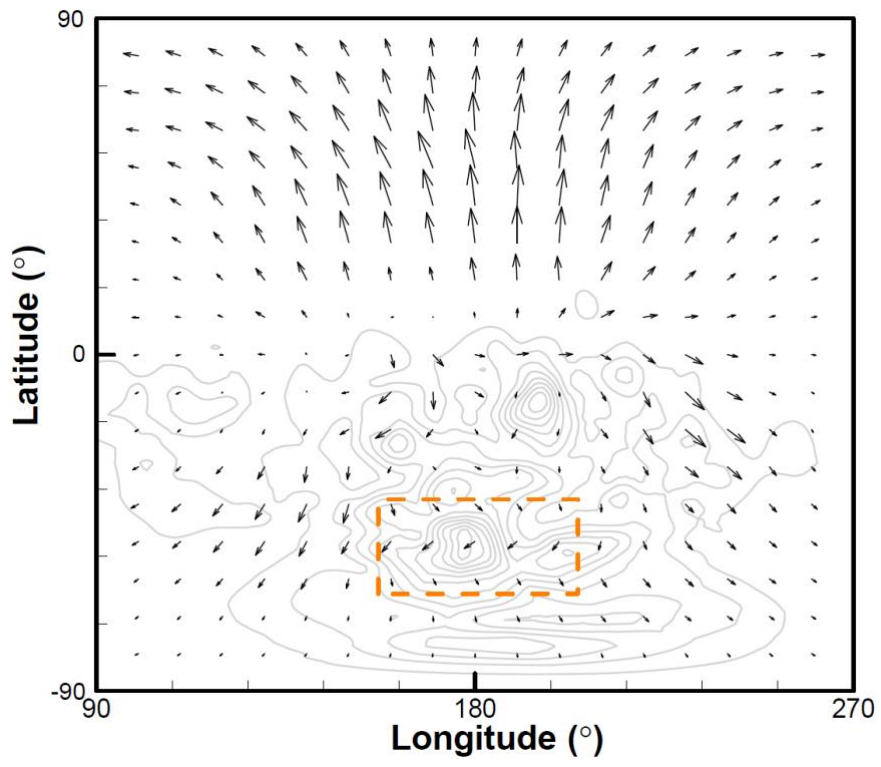
272 Figure 4. Magnetic elevation angle in the longitude-latitude plane at 350 km from results of
273 simulations with ESD model. Black anchor represents the dayside velocity vector of O_2^+ .

274 Figure 5. Distributions of variables resulting from simulation with ESD model at 350 km. (a)
275 magnetic elevation angle in latitude from -30° to -60° and longitude from 160° to 200° . (b)
276 magnetic elevation angle, (c) eastward velocity, (d) eastward EM forces, along the white line of Figure
277 5a at latitude of -50° . Orange and blue highlights represent the outward and inward magnetic field
278 regions respectively.

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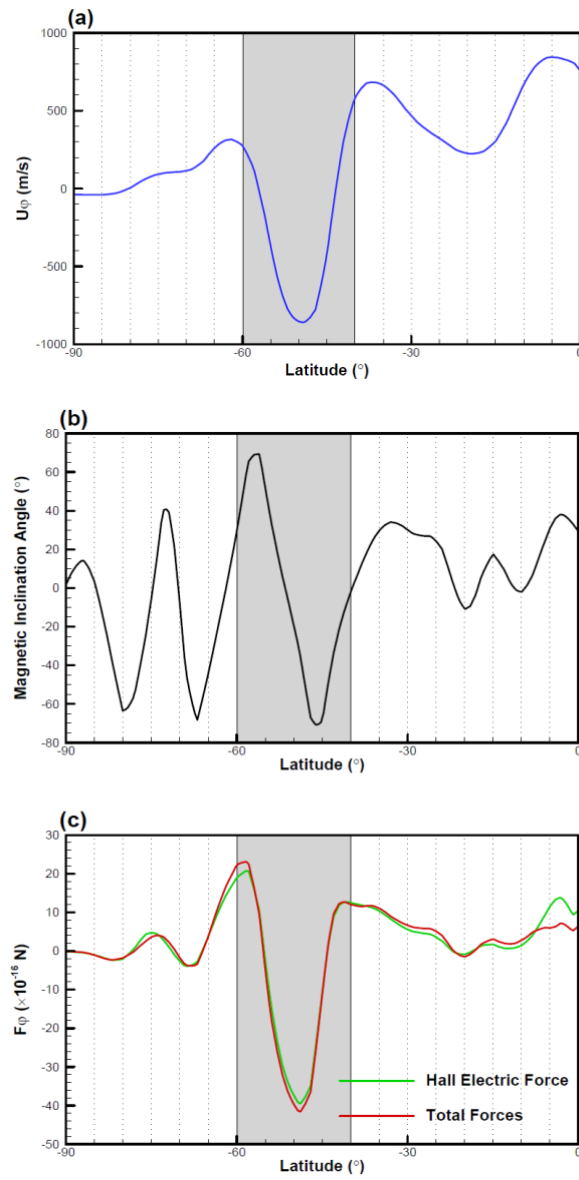
281 Figure 1
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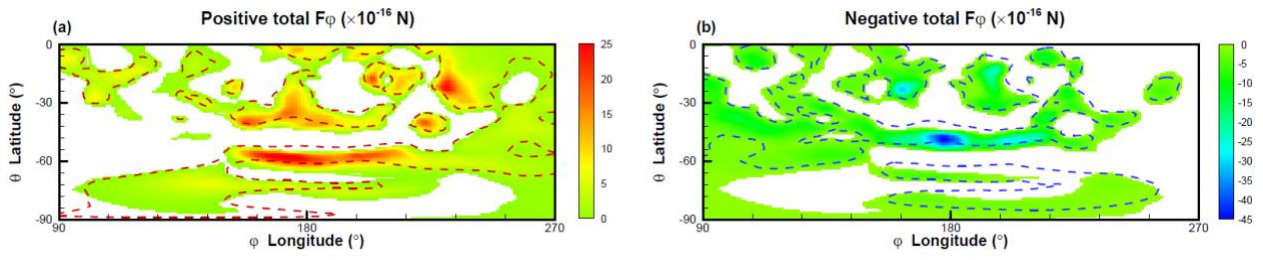
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290 Figure 3

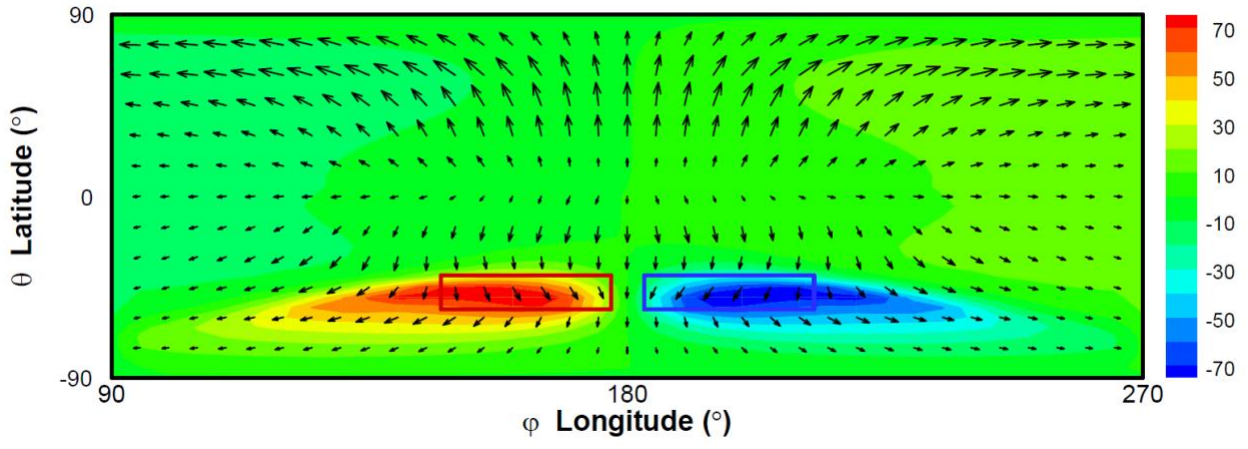
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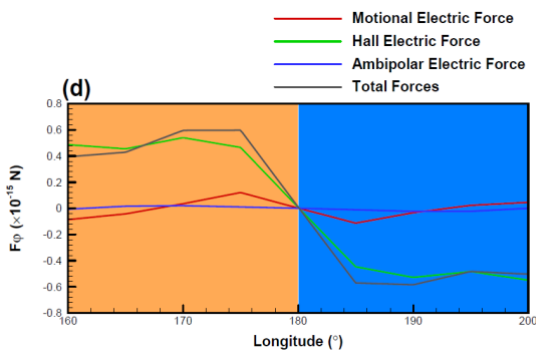
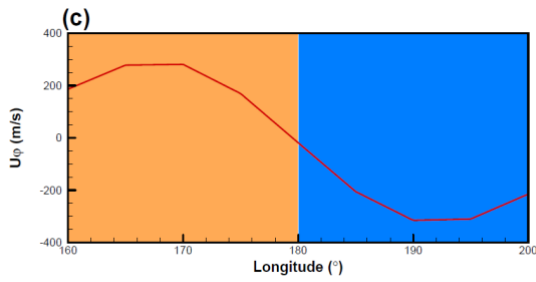
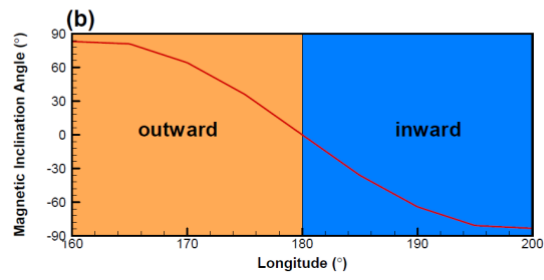
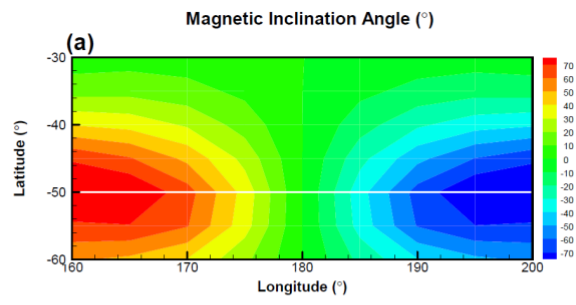
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294 Figure 4
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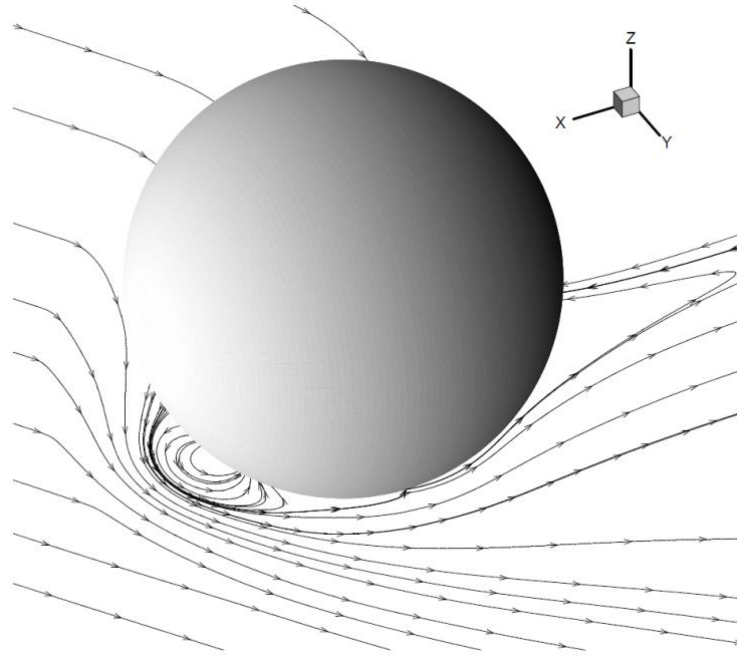
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357 **Appendix A:**

358

359 This appendix depicts the magnetic field topology of the ESD around Mars (Figure A1) and the distributions of the
360 total strength of magnetic field (including both the induced and the crustal magnetic field, Figure A2) and inclination
361 angle (Figure A3) at 350 km, resulting from (a) observation and (b) simulations with the Gao's crustal magnetic
362 field model and (c) the ESD model.



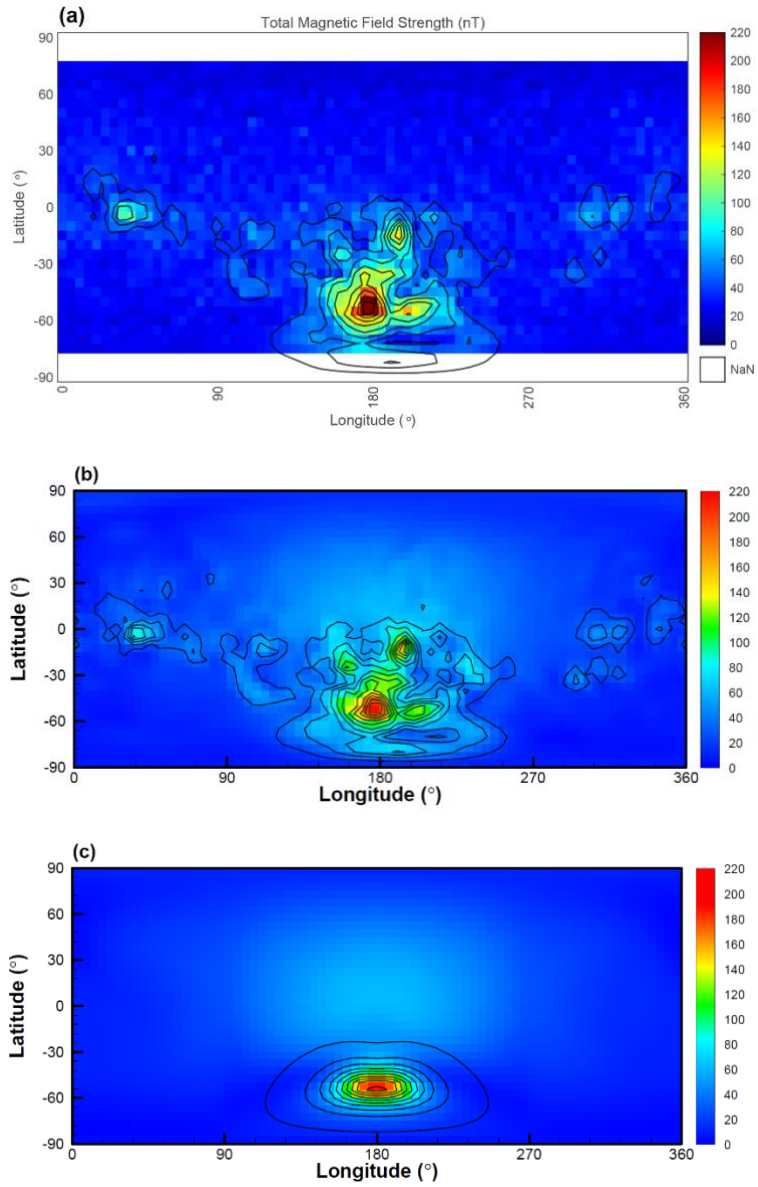
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364 Figure A1. Magnetic field topology around Mars in the case with the ESD model.

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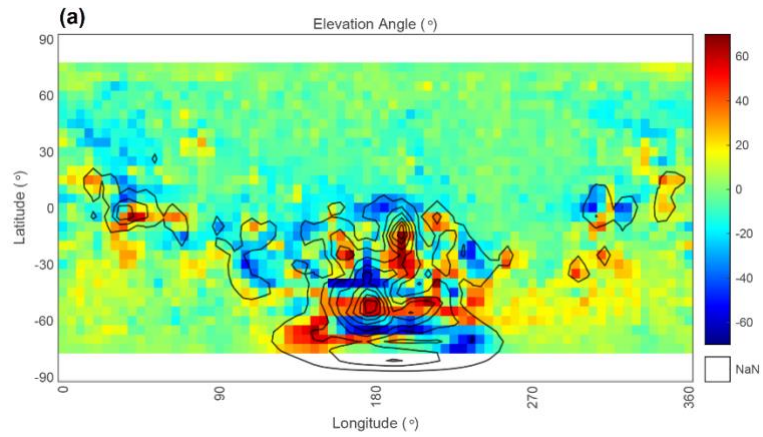
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372 Figure A2. Total strength of magnetic field in the horizontal plane at 350 km, (a) based on the dayside MAVEN
 373 Magnetometer level 2 data and overlapped with isomagnetic lines of crustal field of Gao's model, (b) plotted from
 374 simulation with Gao's crustal field model and overlapped with its isomagnetic lines, (c) plotted from simulation
 375 with the ESD model and overlapped with its isomagnetic lines.

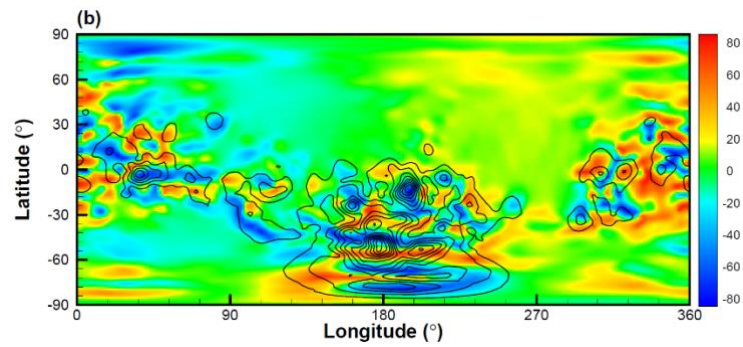
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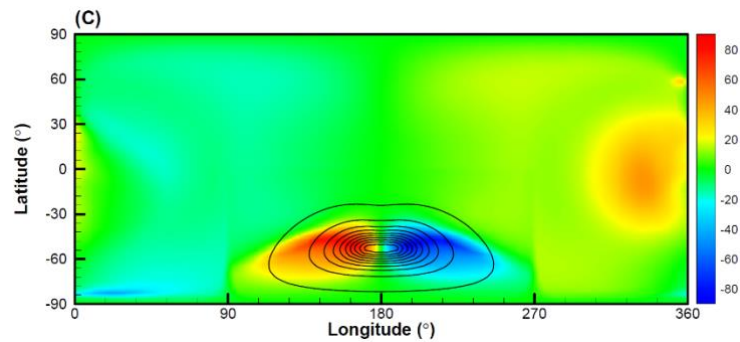
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382 Figure A3. Magnetic elevation angle (also called inclination angle) in the horizontal plane at 350 km, (a) based on
 383 the dayside MAVEN Magnetometer level 2 data and overlapped with isomagnetic lines of crustal field of Gao's
 384 model, (b) plotted from simulation with Gao's crustal field model and overlapped with its isomagnetic lines, (c)
 385 plotted from simulation with the ESD model and overlapped with its isomagnetic lines.

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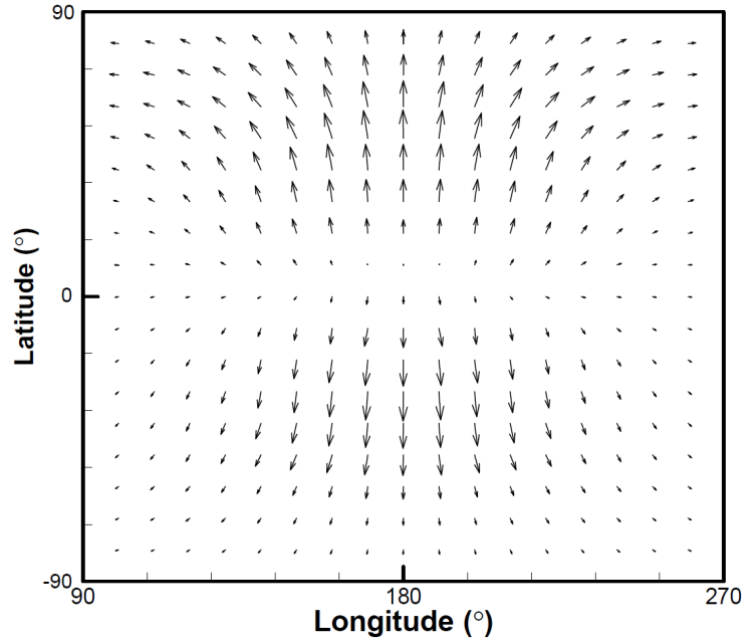
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389 **Appendix B:**

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391 This appendix demonstrates the dayside O_2^+ velocity vector in the horizontal plane at 350 km derived from the multi-
392 fluid MHD model without considering any Martian crustal field case.

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394

395 Figure B1. Dayside distribution of O_2^+ ion velocity vector (black anchor) at 350 km, resulting from simulation
396 without crustal field model.